Figure Captions

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Figure 3c. Anna uses a five tree for the Flag Problem

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Figure 4b. Anna reorganizes her tree with words for the Castle Problem

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